

**A MEMORY MANAGEMENT ALGORITHM FOR TRELLIS DECODERS**

The present patent application claims priority from provisional patent application no. 60/373,246 filed on April 17, 2002.

**BACKGROUND OF THE INVENTION****5    1. *Field of the Invention***

This invention relates generally to the field of digital signal processing and more particularly to signal decoders designed to store selected sequences from which a decoded sequence is ultimately retrieved.

**2. *Background of the Invention***

10        Communications systems such as High Definition Television (HDTV) employ trellis encoding to protect against interference from particular noise sources. Trellis coding requirements for HDTV are presented in sections 4.2.4 – 4.2.6 (Annex D), 10.2.3.9, 10.2.3.10 and other sections of the Digital Television Standards for HDTV Transmission of April 12, 1995 prepared by  
15        the Advanced Television Systems Committee (ATSC). The trellis decoder selects a received symbol sequence as the most likely to be correct, that is, the survivor sequence, according to a signal processing algorithm. The most popular trellis decoding algorithm is the Viterbi algorithm, as described in the paper entitled Convolutional Codes and Their Performance in Communication  
20        Systems, by A. J. Viterbi, published in the I.E.E.E. Transactions on Communications Technology, vol. COM-19, 1971, pp. 751-772. In the Viterbi algorithm, there are two widely known techniques for the storage of the survivor sequences from which the decoded sequence is ultimately retrieved. One technique is known as register exchange and the other technique is  
25        known as traceback. The theory behind the traceback process is described in Architectural Tradeoffs for Survivor Sequence Memory Management in Viterbi Decoders by G. Feygin et al. published in the I.E.E.E. Transactions on

Communications, vol. 41, no. 3, March, 1993. Although relatively simple, the register exchange method requires large power consumption and large area in VLSI implementations, and is therefore restricted to codes having small constraint length. Constraint length is defined as  $K = v + k$ , where  $v$  is the number of memory elements in the trellis encoder and the code rate is  $R = k/n$ . Thus, traceback is the preferred method in the design of moderate to large constraint length trellis decoders.

U.S. Patent No. 5,841,478, entitled CODE SEQUENCE DETECTION IN A TRELLIS DECODER, issued November 24, 1998 to Hu et al., discloses an all-path traceback network coupled to an all-path trace forward network for the selection of the survivor sequence. The described traceback process is performed to a predetermined depth  $T$ , the traceback depth or survivor memory depth, in order to identify a predetermined number of antecedent trellis states. In practice, the traceback interval  $T$  is chosen to provide a sufficient period to permit identification of a merged or converged state. The merged state identifies the data sequence with the greatest likelihood of being the true encoded data. The merged state is the trellis decoded data sequence that is selected as the final output data, chosen from among the several candidate sequences. This traceback process is performed in two stages for traceback intervals of  $T/2$ , known as epochs. The selection of such epochs or traceback subintervals is arbitrary and selectable by the system designer.

The overall memory size required in Hu et al. scheme is  $3/2 * T * N$ , where  $T$  is the predetermined survivor memory depth and  $N$  is the number of states in the trellis. In order to achieve satisfactory decoder performance, the survivor memory depth or traceback depth (or traceback interval)  $T$  is typically four to six times the code constraint length. The value of  $N$  is equal to  $2^v$ , where  $v$  is the number of memory elements in the encoder. The latency, or data decoding delay, associated with the Hu et al. algorithm is  $3/2 * T$ . While the Hu et al. device was implemented in an ATSC HDTV trellis decoder,

which required twelve interleaved decoders, the disclosed technique can be applied to any trellis decoder. Unfortunately, the Hu et al. system is not the most efficient traceback algorithm, and is not as efficient as the register exchange technique with respect to memory size and data decoding delay, or latency. However, it is more efficient than the register exchange algorithm in power consumption and control complexity, as any traceback algorithm would be.

The Hu et al. all-path traceback/forward trace (APTFT) system can be described by the block diagram of Figure 1. The data input 16 to the system consists of a trellis decoder Add-Compare-Select (ACS) unit output per trellis state and per trellis branch, that is, a pointer to the previous state in the trellis. The control inputs consist of clock, enable, reset, any sync signals, and the minimum state per trellis branch. The minimum state per trellis branch is also an ACS output which identifies the state having the minimum path metric (value) at each trellis branch. The control unit generates all of the control signals and read/write addressing of the various memory blocks.

The buffer is a Last In, First Out (LIFO) memory of size  $(T/2) * N$ , which temporarily stores the ACS output. Data is written in order of arrival,  $N$  states at a time, and is read in reverse order during the following epoch. An epoch is characterized by the size of the buffer memory in input samples (trellis branches), that is,  $T/2$  samples. After each read operation, a new data input is written in the same location.

The all-path traceback unit is directed by the control unit to read the buffer memory from the previous epoch, in the reverse order of storage, and trace back through the trellis for an entire epoch of  $T/2$  samples at a time. As it traces back through the trellis, the all-path traceback unit sends a decoded output to the decoded sequence memory for each of the  $N$  states in the trellis. The all-path traceback unit therefore needs  $N$  state pointers to identify the  $N$  surviving paths in the trellis. The  $N$  state pointers are updated for every branch and always point to the previous state in the corresponding path. At

the same time that the all-path traceback unit is reading and processing the ACS data 16, which had been buffered on the previous epoch, the forward trace unit is tracing forward through the trellis with the ACS data 16 of the current epoch.

5           The activities of the various units during each new epoch are depicted in the timing diagram of Figure 2. The input data is written into the buffer memory in normal, forward order and is passed to the all-path traceback unit in reverse order. The decoded output of the all-path traceback unit, for all of the trellis states, is then passed to the decoded sequence memory. This  
10       decoded information is read from the decoded sequence memory two epochs later in reverse order. The two reverse read operations cancel each other, causing the final decoded data to appear in the correct forward order. The two epoch delay in the decoded sequence memory unit necessarily requires a memory size of  $T * N$ .

15           At the end of each epoch, the path selection unit updates and freezes the value of the forward trace pointer,  $P$ , associated with the minimum state path sent by the ACS unit. This pointer is used for a period of one epoch until the next update occurs. At the boundary of an epoch, the forward trace pointer points to the minimum state path and provides the state associated  
20       with this path two epochs earlier. However, as the end of the epoch approaches, the forward state pointer points to the minimum state path at the previous epoch boundary and provides the state associated with this path three epochs earlier. The Hu et al. device actually has two internal pointers ( $P1$  and  $P2$ ) for each state path which are temporally offset from each other  
25       by one epoch. These two pointers will ultimately help identify the trellis decoded bit sequences. The pointer  $P1$  for each state path is updated for every branch with forward trace information, while the pointer  $P2$  is only updated once every epoch. Pointer  $P1$  is the current epoch pointer and pointer  $P2$  is the immediately prior epoch pointer.

Since N states have N survivor state paths, there are  $2 * N$  internal pointers in the forward trace unit. At the end of each epoch, each internal pointer points to the beginning state of the same epoch in the corresponding survivor path. These pointers contribute to create the main pointer P. At the end of an epoch, the pointer P2 receives the value of pointer P1 and then P1 is reset and initiates a forward trace through the trellis during the following epoch. The multiplexer unit uses the forward trace pointer, P, to select one of the N decoded sequences from the decoded sequence memory and to forward the selected decoded bit(s) as its output.

For example, at the end of epoch 3, the forward trace pointer, P, indicates the trellis state associated with the beginning of epoch 2 in the minimum path. The pointer P1 points from the ending state to the beginning state of epoch 3, and the pointer P2 points from the ending state to the beginning state of epoch 2. The pointer P2 is then updated with the value of pointer P1, and pointer P1 is then reset. During epoch 4, the value of pointer P is unchanged and points to the beginning state of epoch 2, and this value will be used by the multiplexer to select the appropriate decoded sequence DD1 in Figure 2, that is being read from the decoded sequence memory out of the N possible sequences. The pointer P2 is frozen or unchanged during epoch 4 and points to the beginning state of epoch 3. The pointer P1 is continuously updated with the forward trace during epoch 4. Similarly, at the end of epoch 4, the forward trace pointer P is updated to point to the beginning state of epoch 3, pointer P2 is updated to point to the beginning state of epoch 4, and pointer P1 is reset. During the entirety of epoch 5, the pointer P selects the correct decoded sequence DD2 in Figure 2, which is being read from the decoded sequence memory. This process continues indefinitely as long as an input signal is available to be processed.

As best understood with reference to Figure 2, the forward trace will process data up to data D3 (data in epoch 3) in order to permit decoding of the data associated with D1, the decoded data being data DD1 (decoded data

from epoch 1), which will occur during epoch 4. Therefore, three epochs are fully processed (epochs 2 and 3 by the forward trace and epoch 1 by the traceback) before the first epoch decoded data DD1 is generated as an output signal. Similarly, in order to output DD2 (decoded data from epoch 2), two epochs (epochs 3 and 4) are processed by the forward trace and one epoch (epoch 2) is processed by the traceback, the process continuing as a sliding window of three epochs at a time. This process implies that the first bit of DD1 has a corresponding survivor memory depth of three epochs or  $3/2 * T$  samples, since the first decoded bit is associated with the beginning of epoch 1 and the pointer P is associated with the end of epoch 3. In contrast, the last bit of DD1 has a survivor memory depth of two epochs, or  $T$ , since the last decoded bit is associated with the end of epoch 1 and the pointer P is associated with the end of epoch 3. Similarly, the first bit of DD2 is associated with a survivor memory depth of  $3/2 * T$ , and the last bit of DD2 is associated with a survivor memory depth of  $T$ . This guarantees that any decoded sequence block (DD1, DD2, DD3 ...) is associated with a survivor memory depth of at least  $T$ .

As the data is processed and decoded by the All-Path Traceback/Forward Trace(APTFT) processor, the memory size will consist of  $T/2 * N$  in the buffer memory plus  $T * N$  in the decoded sequence memory, corresponding to a total of  $3/2 * T * N$ . Additionally, the Hu et al. algorithm needs a total of  $3 * N + 1$  state pointers ( $N$  in the all-path traceback unit and  $2 * N + 1$  in the forward trace unit, that is, pointer P,  $N$  pointers P1 and  $N$  pointers P2). The data decoding delay, or latency, in the Hu et al. device is attributable to a one epoch delay ( $T/2$  samples) in the buffer memory, plus a two epoch delay ( $T$  samples) in the decoded sequence memory. The total latency is thus a three epoch delay, or  $3/2 * T$  samples.

In order to decode a sequence with a survivor memory depth of  $T$ , an efficient algorithm will have the characteristic that each bit has an associated survivor memory depth of  $T$ . Existing traceback algorithms need to decode

entire data blocks per processing cycle with the result that unnecessarily large survivor memory depth exists for all but one bit in the data block. Thus a need exists for an improved trellis decoder memory management scheme in which both memory size and latency values are reduced.

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### BRIEF SUMMARY OF THE INVENTION

The present invention is a trellis decoder system employing an All-Path Traceback/Forward Trace (APTFT) algorithm that reduces memory and latency requirements with respect to the prior art APTFT algorithm. In particular, the present invention discloses a trellis decoder system requiring a memory size of  $T \times N$  (survivor memory depth times the number of trellis states) and a latency of  $T$ , representing a reduction of one third for both parameters without any increase in control requirements and while maintaining the same survivor memory depth  $T$ . This improvement permits the APTFT algorithm to become one of the most efficient traceback techniques. Further, the APTFT algorithm becomes competitive with register exchange algorithms for codes having a small constraint length. The present invention also includes a generalization of the APTFT algorithm which permits greater flexibility in the choice of memory size and latency to satisfy the needs of a particular system.

The present invention can be applied to any trellis decoder system or similar signal processing technique which needs to store and process survivor sequences in order to ultimately generate a decoded or other regimented output sequence. The system may be generalized to one or multiple decoders, concatenated or non-concatenated decoders, decoders with parallel or distributed processing, multiple decoders which are either parallel or serial, interleaved or non-interleaved decoders, and to any type of similar signal processing scheme.

### BRIEF DESCRIPTION OF THE DRAWING

Figure 1 is a simplified block diagram of a prior art All-Path Traceback/Forward Trace (APTFT) system;

Figure 2 is a timing diagram of a prior art APTFT system depicted in Figure 1;

5        Figure 3 is a flow chart of a memory management algorithm operating according to the principles of the present invention;

Figure 4 is a timing diagram showing relationships of data being processed according to the flow chart of Figure 3;

10       Figure 5 is a timing diagram showing relationships of data being processed according to a generalized embodiment of the original APTFT system depicted in Figure 1; and

Figure 6 is a timing diagram of showing relationships of data being processed according to a generalized embodiment of the present invention.

#### DETAILED DESCRIPTION OF THE INVENTION

15       Referring to Figure 1, the simplified block diagram of the prior art All-Path Traceback/Forward Trace (APTFT) system permits an understanding of the present invention. The functional blocks depicted in Figure 1 perform in the same manner for the purposes of the present invention with the exception of the Forward Trace & Path Selection unit 17. The present invention exploits  
20       the characteristics of the forward trace to simplify operation of the prior system. As earlier mentioned, at the conclusion of each epoch the Forward Trace & Path Selection unit updates and freezes the forward trace pointer, P, which is associated with the minimum trellis path state sent by the Add-Compare-Select (ACS) unit. The pointer P is then used for the entire  
25       duration of an epoch to select the optimum decoded sequence from the decoded sequence memory. As a result, the first decoded bit of an epoch is



associated with a survivor memory depth of  $3/2 * T$ , and the last decoded bit is associated with a survivor memory depth of  $T$ .

In the present invention, at the conclusion of each epoch the forward trace pointer,  $P$ , is not frozen, but is instead allowed to continuously update its value throughout the decoding process. As earlier stated, pointer  $P1$  is continuously updated by the forward trace during an epoch while the pointer  $P2$  is only updated at the end of an epoch. Both pointers  $P1$  and  $P2$  for each trellis state, together with the minimum path value received from the ACS unit, contribute to create the value of pointer  $P$ . By continuously updating pointer  $P$  for every data sample, the value of pointer  $P$  will reflect the continuously updated value of pointer  $P1$  and therefore reflect the continuous forward trace process through the trellis. In this manner the survivor memory depth is a sliding window of constant size  $T$  propagating through the trellis.

As a result of continuously updating the value of pointer  $P$ , the decoded sequence memory, which receives the decoded data sequences from the all-path traceback unit 12 for all of the trellis states, needs to make its data available to the multiplexer 14 one epoch later rather than two epochs later. The one epoch delay requires a memory size of  $(T/2) * N$ , rather than  $T * N$  (for a two epoch delay), thereby permitting a fifty percent decrease in the size of the decoded sequence memory 13.

As the data 16 is processed and decoded by the modified APTFT processor just described, the memory size will consist of  $(T/2) * N$  for the buffer memory 15, plus  $(T/2) * N$  for the decoded sequence memory 13, corresponding to a total memory requirement of  $T * N$ . Further, there is a one epoch delay ( $T/2$  samples) attributable to the buffer memory 15 and a one epoch delay ( $T/2$  samples) attributable to the decoded sequence memory 13, resulting in a total latency that is equal to a two epoch delay ( $T$  samples). The modified APTFT processor of the present invention requires a total of  $3 * N + 1$  trellis state pointers based on  $N$  pointers in the all-path traceback unit 12

and  $2 * N + 1$  pointers in the forward trace unit 17, that is, pointer P, N pointers P1 and N pointers P2.

Referring also to Figure 3, the data processing steps of the present invention can be appreciated. At step 1, prior to the start of each epoch, the values of the pointers P2 are updated with the data in the equivalent state pointers P1. After the new epoch starts at step 2, the current input data of step 3 is buffered at step 4 and forward traced at step 7. Concurrently data corresponding to a previous epoch is retrieved from the buffer and traced back to generate the decoded data at step 5. The decoded data is then written, at step 6, into the decoded sequence memory. The forward trace performed on the current data at step 7 determines the values of pointers P1. At step 8 the values of pointers P1 together with the stored values of pointers P2 and the minimum path state information from the ACS (acs\_select) are used to generate the value of pointer P. Also at step 6 the value of pointer P is used to identify the decoded data from the two previous epochs associated with the minimum trellis path state, which is then retrieved from the decoded sequence memory. At step 9 the decoded data is forwarded to the next stage and at step 10 the process (steps 3 through 9) is repeated for the entire epoch. When the epoch is completed, step 11 restarts the algorithm (steps 1 through 10) for the next epoch.

Referring also to Figure 4 the timing relationships resulting from the operation of the above algorithm can be understood. The forward trace operation processes complete epochs up to the data in epoch 2, as shown by cell 18. This permits decoding of data D1, that is, the data in epoch 1, which will become the decoded data DD1 from epoch 1 that is read in epoch 3 in cell 19. Therefore, before the first epoch decoded data DD1 is produced as an output from cell 19, two epochs have been fully processed, namely, epoch 2 by the forward trace (cell 18) and epoch 1 by the traceback (cell 20). When the forward trace is processing branch  $j$  ( $1 < j < T/2$ ) of epoch 3, pointer P1 will point from the present state to the beginning state of epoch 3, pointer P2

will point from the end to the beginning state of epoch 2, and the resultant pointer P will point from the present state to the beginning state of epoch 2. Simultaneously, the decoded data sequence DD1 (cell 19) is available at the multiplexer output 21. As pointers P1 and P progress through the epoch 3 forward trace (cell 22), the output of decoded data bits progresses through branches 1 to  $T/2$ . Therefore, the dimension of the survivor memory depth sliding window is a constant value of T, which is equal to the dimension from branch j of epoch 3 to branch j of epoch 1, where  $1 < j < T/2$ . In summary, the total memory size of T and the total latency of two epochs represent a reduction of 33% over the prior art APTFT memory management scheme at no additional control complexity.

The APTFT algorithm of the present invention attains advantages known to both traceback and register exchange algorithms. Therefore, it is useful to compare it with the prior art described in Architectural Tradeoffs for Survivor Sequence Memory Management in Viterbi Decoders by G. Feygin et al. published in the I.E.E.E. Transactions on Communications, vol. 41, no. 3, March, 1993.

Table 1 depicts some of the differences and similarities between the APTFT algorithm of the present invention and the prior art register exchange algorithm.

IMPROVED APTFT ALGORITHM	REGISTER EXCHANGE ALGORITHM
Survivor Memory Depth is equal to $T$	Survivor Memory Depth is equal to $T$
Latency is equal to $T$	Latency is equal to $T$
Memory size is equal to $T * N$	Memory size is equal to $T * N$
Memory is Random Access Memory	Memory is complex, dual port, plus a two-to-one multiplexer, plus the interconnections between individual memory elements
Memory read/write operations per trellis branch is equal to $2 * N$	Memory read/write operations per trellis branch is equal to $N * T$
Power consumption is relatively small	Power consumption is relatively large
Additional control in the traceback/forward trace units	No additional control

**Table 1**

Both algorithms have the same latency and memory size for a similar survivor memory depth, which is not generally accomplished by previous traceback algorithms. The improved APTFT protocol requires additional control in the traceback unit 12 and forward trace unit 17, as represented by the need for  $3 * N + 1$  state pointers, although the relative complexity of each pointer is small. In contrast, the use of the register exchange algorithm introduces additional complexity in the memory required, with the need for a two to one multiplexer for each memory element and the interconnections between the memory elements. Further, the present invention reads and writes to only  $2 * N$  memory elements per trellis branch, whereas the register exchange algorithm must read and write to all  $N * T$  memory elements per trellis branch. This latter characteristic results in large power consumption for the register exchange system, which becomes a limitation as the code constraint length increases. The additional state pointers of the present invention represent an acceptable cost in exchange for the use of a simple random access memory and reduced power consumption. In summary, the present invention is competitive with the register exchange algorithm for small

constraint length codes and becomes more efficient than the register exchange system as the constraint length of the code is increased.

Table 2 portrays some of the differences between the present invention and another traceback system, the so called k-pointer even algorithm, which is exemplary of the complexity and efficiency of typical prior art traceback systems. Another traceback technique known as the k-pointer odd algorithm is similar in complexity and efficiency and will not be explicitly addressed.

IMPROVED APTFT ALGORITHM	k-POINTER EVEN ALGORITHM
Survivor memory depth is equal to T	Survivor memory depth is equal to T
Latency is equal to T	Latency is equal to $2 * T * k / (k - 1)$
Memory size is equal to $T * N$	Memory size is equal to $2 * T * N * k / (k - 1)$
Number of state pointers is equal to $3 * N + 1$	Number of state pointers is equal to k

**Table 2**

The best latency and memory size achieved by the k-pointer even algorithm occurs as the value of k approaches T, being approximately twice the corresponding latency and memory size of the present invention. When k is at its smallest value of  $k = 2$ , the latency and memory size of the k-pointer even algorithm is four times the corresponding values of the present invention. The present invention therefore offers a considerable advantage in memory use and latency parameters. These improvements are achieved at the expense of extra control requirements that take the form of additional trellis state update pointers, which ultimately represent a limitation for large constraint length codes.

Table 3 depicts some of the differences between the implementation of the present invention and the one-pointer algorithm of the prior art. The one-pointer algorithm is a small latency, small memory size traceback algorithm. Another traceback technique known as the even-hybrid algorithm is similar in complexity and efficiency and will not be explicitly addressed.

IMPROVED APTFT ALGORITHM	ONE-POINTER ALGORITHM
Survivor memory depth is equal to $T$	Survivor memory depth is equal to $T$
Latency is equal to $T$	Latency is equal to $T * (k + 1)/(k - 1)$
Memory size is equal to $T * N$	Memory size is equal to $T * N * (k + 1)/(k - 1)$
Memory read/write operations for each trellis branch is equal to $2 * N$	Memory read/write operations for each trellis branch is equal to $(k + 1) * N$
Speed of read/write controls is equal	Read control is $k$ times faster than write control
Number of trellis state update pointers is $3 * N + 1$	Number of trellis state update pointers is 1

**Table 3**

The best latency and memory size achieved by the one-pointer algorithm occurs as the value of  $k$  approaches the value of  $T$ , and is approximately equal to the latency and memory size of the present invention. When the value of  $k$  is smallest, at  $k = 2$ , the latency and memory size of the one-pointer system is three times greater than that of the present invention. Thus the one-pointer algorithm approaches the performance of the present invention only when the value of  $k$  is large. An advantage of the one-pointer algorithm is its need for only one state pointer as compared to the  $3 * N + 1$  state pointers of the present invention. However, the need for a single pointer is achieved at the cost of a relatively more complex read/write control, because the read operations occur at a rate that is  $k$  times faster than the write operations. When the value of  $k$  is large, that is, when the value of  $k$  approaches the value of  $T$ , the number of memory read/write operations of the one-pointer algorithm approaches the number of such operations performed by the previously discussed register exchange system, resulting in a similarly large power consumption for the one-pointer system.

A generalized version of the original (prior art) APTFT system can be understood with reference to Figure 1. The generalized embodiment derives its name from the definition of an epoch. Specifically, an epoch is not

necessarily limited to a size equal to half of the memory depth, or  $T/2$ .

Rather, an epoch may be generally defined as equal to  $T/q$ , where  $q$  is an integer having a value defined by the inequality  $2 < q < T$ .

In the case of the general epoch value of  $T/q$ , the original APTFT relationships depicted in Figure 2 are modified in several ways. First, the size of buffer 15 is  $(T/q) * N$  instead of  $(T/2) * N$ . Second, the decoded sequence memory 13 receives the decoded data sequences from the all-path traceback unit 12, for all of the trellis states, and makes the decoded data available to multiplexer 14 after  $q$  epochs, rather than two epochs later. The  $q$  epoch delay requires the same memory size of  $T * N$ .

Reference to Figure 5 will permit an understanding of the timing relationships that occur in the generalized original APTFT algorithm. The forward trace pointer,  $P$ , points to the minimum trellis path and provides the trellis state associated with the minimum path existing  $q$  epochs earlier, rather than two epochs earlier. The generalized design requires  $q$  internal pointers per trellis state in the forward trace, rather than two internal pointers, offset in time by intervals of one epoch. By the end of one epoch, each internal pointer  $P_1, P_2, \dots, P_q$ , points to the beginning state of the corresponding epoch and trellis state path, and all internal pointers contribute to create the main pointer  $P$ . As seen in Figure 5, the forward trace will process data up to  $D_q + 1$  (cell 24), in order to permit decoding of the data associated with  $D_1$ , which therefore becomes  $DD_1$  (cell 26), the decoding occurring in epoch  $q + 2$  (cell 25). Therefore,  $q + 1$  epochs are fully processed (epochs 2 up to  $q + 1$  by the forward trace, and epoch 1 by the traceback) before the first epoch decoded data  $DD_1$  is provided as an output (cell 25). The first bit of any decoded sequence block  $DD$  is associated with a memory depth of  $(q + 1) * T/q$ , and the last bit of the decoded sequence block is associated with a survivor memory depth of  $T$ .

As the data is processed by the generalized original APTFT processor, the memory size will consist of  $T/q * N$  in the buffer memory plus  $T * N$  in the

decoded sequence memory, corresponding to a total memory size of  $(q + 1)/q * T * N$ . Further, the generalized original APTFT algorithm needs a total of  $(q + 1) * N + 1$  state pointers ( $N$  in the traceback unit and  $q * N + 1$  in the forward trace unit). There is a one epoch delay ( $T/q$  samples) in the buffer memory,  
5 plus a  $q$  epoch delay ( $T$  samples) in the decoded sequence memory, resulting in a total latency corresponding to a  $(q + 1)$  epoch delay, or  $(q + 1) * T/q$  samples.

In the generalized original APTFT algorithm, the memory size and latency decrease as  $q$  increases, at the cost of additional internal pointers in  
10 the forward trace unit. Depending on the system, an appropriate choice of  $q$  can be found which will minimize overall complexity, and for which the increase in the number of internal pointers is a small cost compared to the decrease in memory size and latency. This is generally true since the number of internal pointers is proportional to the constraint length, while the memory  
15 size grows exponentially with the constraint length. The optimum case as far as latency occurs when  $q$  is equal to  $T$ , resulting in a latency of  $T + 1$ , which is the minimum possible for such a system. The memory size will then be  $(T + 1) * N$  and the number of internal pointers will be  $(T + 1) * N + 1$ . In this case the epoch consists of just one sample and the buffer memory consists of  $N$   
20 registers.

The generalized original APTFT technique can be advantageously applied to any trellis decoder system including one or more multiple decoders, decoders with either parallel or distributed data processing, serial or parallel multiple decoders, whether interleaved or not, and to any type of similar signal  
25 processing application.

A generalized embodiment of the improved APTFT system is also realized by redefining an epoch as being equal to  $T/q$ , where  $q$  is an integer having a value defined by the inequality  $2 < q < T$ . In the case of the generalized epoch value of  $T/q$ , the changes to the improved APTFT system  
30 include altering the size of buffer 15 from  $(T/2) * N$  to  $(T/q) * N$ . The decoded



sequence memory 13 receives the decoded data sequences from the all-path traceback unit 12, for all of the trellis states, and makes the decoded data available to multiplexer 14 after  $q - 1$  epochs, rather than one epoch later. The  $q - 1$  epoch delay requires a memory size of  $(q - 1)/q * T * N$ .

5           Reference to Figure 6 will permit an understanding of the timing relationships that occur in the generalized improved APTFT system. The forward trace pointer, P, points to the minimum path and provides the trellis state associated with the minimum path existing  $q - 1$  epochs earlier, rather than one epoch earlier. The generalized design requires  $q$  internal pointers  
 10 per trellis state in the forward trace unit, rather than two internal pointers, offset in time by intervals of one epoch. By the end of one epoch, each internal pointer P1, P2, ...Pq, points to the beginning state of the corresponding epoch and state path, and all internal pointers contribute to create the main pointer P. All internal pointers except P1 are updated only at  
 15 the end of an epoch, and their value remains unchanged during the following epoch. Pointer P1 is reset at the beginning of each epoch and is continuously updated throughout the forward trace.

As seen in Figure 6, the forward trace will process complete epochs up to Dq (cell 28), in order to permit decoding of the data associated with D1,  
 20 which therefore becomes DD1 (cell 29), the decoding occurring in epoch  $q + 1$  (cell 30). Therefore,  $q$  epochs are fully processed (epochs 2 up to  $q$  by the forward trace, and epoch 1 by the traceback) before the first epoch decoded data DD1 is provided as an output (cell 30). When the forward trace is processing branch  $j$  ( $1 < j < T/2$ ) of epoch  $q + 1$ , pointer P1 will point from the  
 25 present state to the beginning state of epoch  $q + 1$ . Pointer P2 will point from the end to the beginning state of epoch  $q$ , pointer  $q$  will point from the end to the beginning state of epoch 2, and pointer P will point from the present state to the beginning state of epoch 2. At the same time, the decoded sequence DD1 is available at the multiplexer output 21. As pointers P1 and P progress  
 30 through the epoch  $q + 1$  forward trace, the decoded output bits progress

through branches 1 to  $T/2$ . Therefore, the dimension of the survivor memory depth sliding window is a constant value of  $T$ , which is equal to the dimension from branch  $j$  of epoch  $q + 1$  to branch  $j$  of epoch 1, where  $1 < j < T/2$ .

As the data is processed by the generalized improved APTFT processor, the memory size will consist of  $T/q * N$  in the buffer memory plus  $(q - 1)/q * T * N$  in the decoded sequence memory, corresponding to a total memory size of  $T * N$ . Further, the generalized improved APTFT algorithm needs a total of  $(q + 1) * N + 1$  state pointers ( $N$  in the traceback unit and  $q * N + 1$  in the forward trace unit). There is a one epoch delay ( $T/q$  samples) in the buffer memory, plus a  $(q-1)$  epoch delay  $((q - 1) * T/q$  samples) in the decoded sequence memory, resulting in a total latency corresponding to a  $q$  epoch delay, or  $T$  samples.

In the generalized improved APTFT algorithm, the memory size and latency remain constant as  $q$  increases, at the cost of additional internal pointers in the forward trace unit. Therefore, there is no cost advantage in increasing  $q$  beyond 2. However, although not optimal, the generalized improved algorithm for  $q > 2$  offers enough flexibility to satisfy different system requirements, which may incur from restrictions in memory size, for example.

The generalized improved APTFT technique can be advantageously applied to any trellis decoder system including one or more multiple decoders, decoders with either parallel or distributed data processing, serial or parallel multiple decoders, whether interleaved or not, and to any type of similar signal processing application.